

Angular correlation of the two gamma rays produced in the thermal neutron capture on gadolinium-155 and gadolinium-157

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The ANNRI-Gd collaboration studied in detail the single γ -ray spectrum produced from the thermal neutron capture on ^{155}Gd and ^{157}Gd in our previous publications. Gadolinium targets were exposed to a neutron beam provided by the Japan Spallation Neutron Source (JSNS) in J-PARC, Japan. In the present analysis, one new additional coaxial germanium crystal was used in combination with the 14 germanium crystals in the cluster detectors to study the angular correlation of the two γ rays emitted in the same neutron capture. We present for the first time angular correlation functions for two γ rays produced during the electromagnetic cascade transitions in the (n, γ) reactions on ^{155}Gd and ^{157}Gd . As expected, we observe mild angular correlations for the strong, but rare transitions from the resonance state to the two energy levels of known spin-parities. Contrariwise, we observe negligibly small angular correlations for arbitrary pairs of two γ rays produced in the majority of cascade transitions from the resonance state to the dense continuum states.
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Subject Index C42, C43, D03, F20, H20

1. Introduction

The gadolinium (Gd) nucleus is one of the few stable nuclei (Cd, Sm, Gd) featuring unusually large cross sections and resonance enhancements for thermal neutron capture [1–4]. The two gadolinium isotopes ^{157}Gd and ^{155}Gd possess the largest neutron capture cross sections among the stable nuclei [1]. The element has been used as a neutron absorber in liquid-scintillator-based detectors for neutrino oscillation experiments [5–13], a neutrino-flux monitor experiment [14], and even medical science [15]. The application of Gd-loaded detectors for tagging neutrons

has been recently extended to direct dark matter search experiments [16,17]. The identification of neutrons produced from the inverse beta decay with large efficiency is crucial for the detection of Supernova Relic Neutrinos (SRN) in a Gd-loaded water Cherenkov detector like Super-Kamiokande [18–20]. Upon neutron capture, the Gd isotopes ^{157}Gd and ^{155}Gd release a cascade of γ rays with a total energy of 7937 keV for ^{158}Gd and 8536 keV for ^{156}Gd . Due to the Cherenkov threshold applying for the detection of the multiple Compton electrons produced by these γ rays in the Super-Kamiokande detector, a precise knowledge and understanding of the cascade γ -ray energies is absolutely necessary in order to model the neutron capture efficiency with Monte Carlo simulations.

In our previous publications [21,22], we reported measurements of the single γ -ray spectra produced from the thermal neutron capture on targets comprising a natural Gd film and gadolinium oxide powders enriched with ^{155}Gd and ^{157}Gd , where we used the two cluster detectors of the ANNRI spectrometer at J-PARC, covering 15% of the solid angle with respect to the target. Moreover, we showed that our Monte Carlo simulation (ANNRI-Gd Model) agreed with our measured spectra reasonably well. We first identified the prominent photopeaks above 5 MeV in the single spectrum and found the secondary transitions associated with each primary photopeak. We listed 12 and 15 primary γ rays for ^{155}Gd and ^{157}Gd , respectively, and also identified the secondary γ rays. Those ‘discrete’ γ rays constitute 3%–7% of the total γ rays. However, most of the γ rays result from the dense ‘continuum’ states.

In the present paper, we report on the angular correlations between the two γ rays for some selected discrete and continuum transitions in the ^{155}Gd and $^{157}\text{Gd}(n, \gamma)$ reactions. One new additional coaxial germanium crystal was introduced in the analysis in combination with the 14 germanium crystals in the cluster detectors to study the angular correlation of the two γ rays emitted in the same neutron capture. Although the solid angle covered by the single coaxial detector for a γ ray emitted in the target is only 1.0% and that covered by the cluster detectors is 15%, the coaxial detector has played an essential role in the analysis and it has made it possible to present the result of the angular correlation of the two γ rays over the entire region of $\cos\theta_{12}$: while the range of $\cos\theta_{12}$ for the angle θ_{12} between the two γ rays measured by the cluster detectors is limited to $-1 < \cos\theta_{12} < -0.6$ and $0.6 < \cos\theta_{12} < 1.0$, a new range $-0.4 < \cos\theta_{12} < 0.4$ has been covered by measuring the angle θ_{12} between the one coaxial detector and another crystal of the cluster detectors. We show a comparison between our data and the expected angular correlations. The theoretical calculations for the electromagnetic cascade transitions and the angular correlation function can be found elsewhere [23–25].

It is not only essential for many detectors using gadolinium [5–14,16,17,19] to improve their detector simulations of the energy spectra of the γ rays for high-accuracy analysis, but also very important to understand the basic feature of the angular correlation of the two γ rays produced from the discrete and continuum transitions in thermal neutron capture reactions. Recently, a Monte Carlo simulation called the FIFRELIN code [26] has been developed for the STEREO experiment [10] which takes into account the angular correlations in cascade transitions. Thus, our new data of the angular correlations measured in the ^{155}Gd and $^{157}\text{Gd}(n, \gamma)$ reactions are expected to improve and validate the detector simulation.

2. Experiment

2.1. Experiment and data collection

The data presented in this analysis were recorded in December, 2014, with the ANNRI germanium (Ge) spectrometer at the Materials and Life Science Experimental Facility (MLF) of J-PARC. The MLF provides a pulsed neutron beam with energies from a few meV up to 100 keV. Gadolinium oxide powder targets (Gd_2O_3) enriched with ^{155}Gd (91.85%) and ^{157}Gd (88.4%) were placed inside the ANNRI Ge spectrometer, which consists of two basic parts: two cluster detectors placed perpendicular to the beam pipe, and eight coaxial detectors placed in a horizontal plane containing the beam pipe and the gadolinium target [27–30]. The two cluster detectors and only one of the coaxial detectors were operational during the experiment. A complete description of our experiment and the analysis method, using the two cluster detectors, which consisted of a total of 14 Ge crystals, can be found in our previous publications [21,22].

In the present analysis, we analysed the data recorded by the single coaxial detector in the horizontal plane in addition to the two cluster detectors. The overall view of the ANNRI spectrometer including both the cluster detectors and the coaxial detectors is shown in Fig. 1(a); the detailed geometry of the single coaxial detector and its lead shield is shown in Figs. 1(b) and 1(c). The energy threshold for γ detection of the coaxial detector was about 300 keV. The other seven coaxial crystal detectors were undergoing repair and were not operational during our experiment. The single coaxial detector covers 1.0% and the cluster detectors cover about 15% of the 4π solid angle for a γ ray from the target. As already stressed in the introduction, the present measurement of the angular correlation of the two γ rays over the entire region of $\cos\theta_{12}$ has been made possible by the combination of the coaxial detector and the cluster detectors.

2.2. Calibration

The coaxial detector is self-contained with an individual aluminum protective case. In addition to the protective layer, it is also protected by a lead collimator to reduce the solid angle of γ rays produced outside the gadolinium target. LiH was filled inside the lead collimator to reduce the neutron background. With the use of cluster detectors alone, the angular correlation measurements would have been quite limited. The addition of the one coaxial detector allows for a much greater angular coverage, and substantially larger statistics for the angular correlation analysis. The efficiency of the coaxial detector was estimated with the same method as used for the cluster detectors. This method is described in detail in our previous publications [21,22]. In brief, we used radioactive calibration sources, e.g. ^{60}Co , ^{137}Cs , and ^{152}Eu , as well as the prompt γ rays produced by the neutron capture reaction $^{35}\text{Cl}(n, \gamma)^{36}\text{Cl}$ in the energy range between 0.1 MeV and 9 MeV. To calculate the γ -ray detection efficiency of the coaxial detector, we divide the number of γ rays detected within the photopeaks by the number of γ rays expected due to the solid angle of our detector, corrected by the lifetime of our data acquisition.

The efficiency values obtained for the coaxial detector are shown in Fig. 2 as a function of γ -ray energy and are compared to our Geant4 Monte Carlo simulation (dashed-dotted curve) that includes the full geometry and materials of the ANNRI detector. The absolute normalization of our data to the simulation was obtained using the 7414-keV line of the capture reaction $^{35}\text{Cl}(n, \gamma)^{36}\text{Cl}$. The size of the error bars is determined by the statistics of the data and the Monte

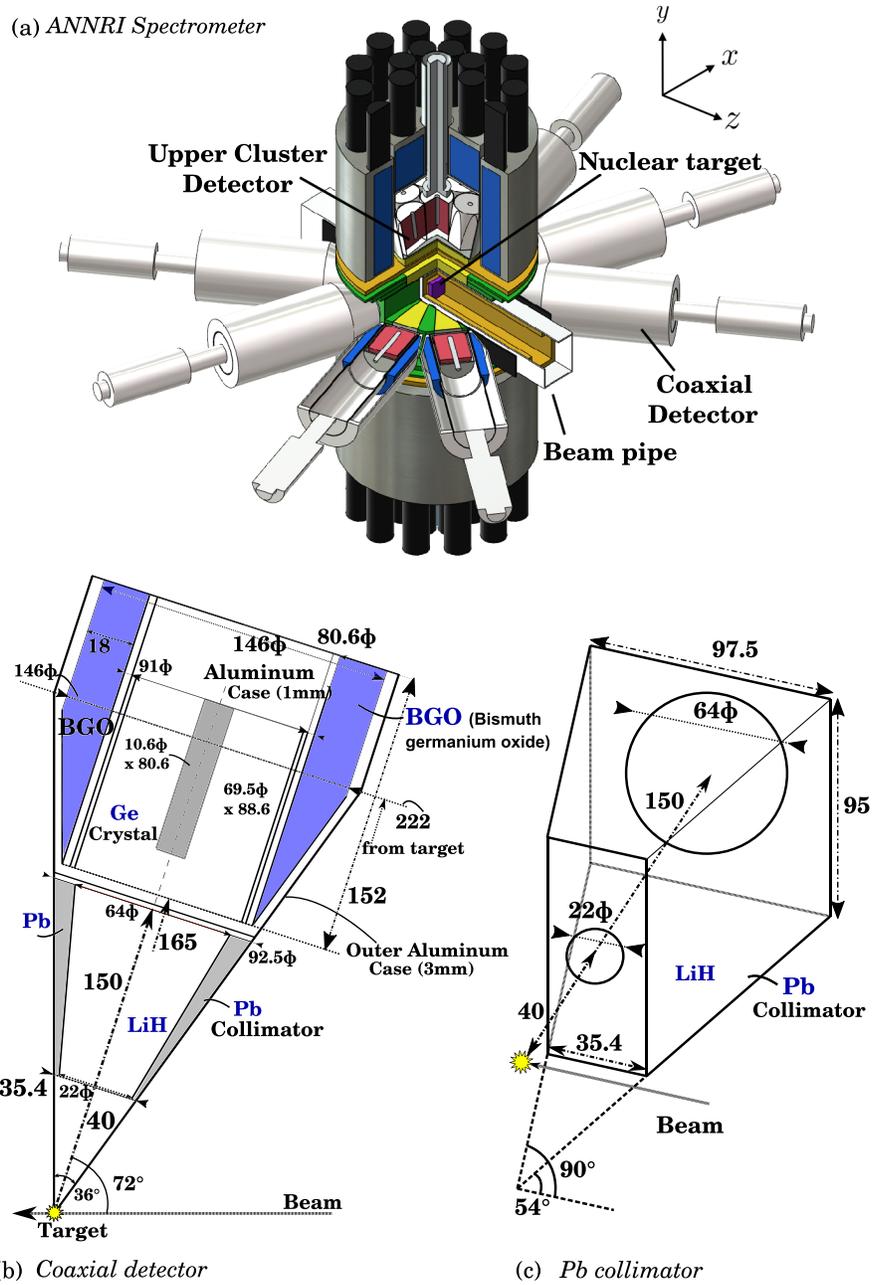


Fig. 1. ANNRI spectrometer.

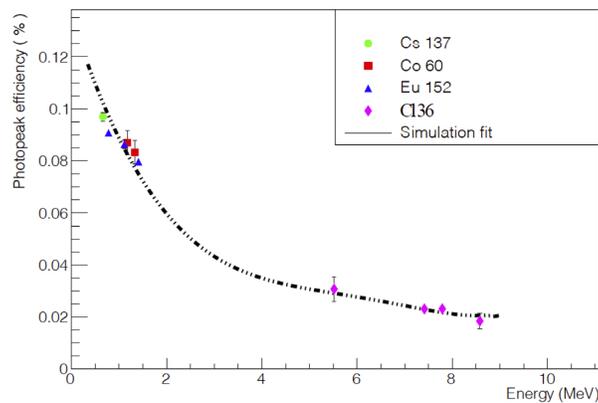


Fig. 2. Efficiency measurements for the coaxial detector compared with simulations (dashed-dotted curve).

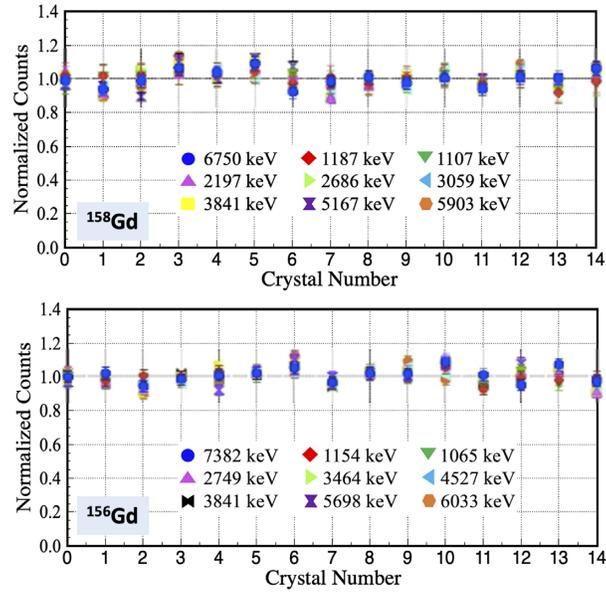


Fig. 3. Normalized counts of various photopeaks for different energy ranges and for each crystal of the 15 detectors. The top and bottom plots are for the counting rates of various γ rays from ^{158}Gd and ^{156}Gd , respectively.

Carlo simulation. The agreement between our calibration data and the detector simulations (dashed-dotted curve) is satisfactory.

In our previous publications [21,22], we studied the uniformity of the counting rate measured by each crystal of the cluster detectors using the data of radioactive calibration sources. Here, we present a new analysis of the uniformity of both the two clusters and the coaxial detector using the prominent photopeaks produced by exposing the gadolinium targets. For a given photopeak, we calculated for each crystal the ratio of the number of raw data events divided by the expected numbers after taking into account the efficiency, the solid angle, and the relative intensity of each photopeak. Figure 3 shows the results for ^{158}Gd (top) and ^{156}Gd (bottom). In the histograms, the detector number 0 represents the coaxial detector while the numbers 1–14 correspond to the crystals of the two cluster detectors. The figures show a very good uniformity between the 15 detectors over an energy range of 1 MeV up to 7 MeV. The variation of the ratios by about 10% is taken as a measure of the systematic uncertainties of the counting efficiencies. This uniformity of the measured rates over the two cluster detectors and the coaxial detector is an essential prerequisite for the present analysis of the angular correlations.

2.3. Data selection and the definition of the angular correlation function $W(\theta)$

As in our previous publications [21,22], we classify events by assigning a multiplicity value M and a hit value H to each event. We defined the multiplicity M as the combined number of isolated subclusters of hit Ge crystals at the upper and the lower cluster detectors. If the coaxial crystal is hit, the values of M and H are both increased by 1, since the hit is always isolated. The multiplicity M represents the number of observed γ rays and the hit value H represents the total number of Ge crystals hit in the event. We select events categorized as M2H2 and M2H3 to study the angular correlations of two γ rays.

We define the angular correlation function $W(\theta_{12})$ using a sample of two γ rays detected by the two crystals (i, j) , where θ_{12} is the angle between the two hit crystals (i, j) [23–25]. For

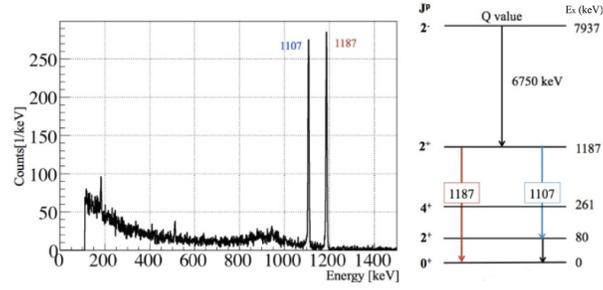


Fig. 4. Energy spectra of γ rays measured by the ANNRI detector (left) and illustration of the two- and three-step γ -ray cascades (right) of ^{158}Gd after thermal neutron capture.

thermal neutron capture on ^{158}Gd , a typical process producing two γ rays is a two-step or three-step cascade transition in the deexcitation of the initial state of 7937 keV (2^-). As illustrated in Fig. 4 (right), two γ rays of 6750 keV and 1187 keV, or three γ rays of 6750 keV, 1107 keV, and 80 keV, are produced in these transitions. Figure 4(left) shows the energy of the second γ ray in case the first γ ray of 6750 keV is tagged, using the M2H2 (multiplicity 2) sample. Two peaks corresponding to the γ rays of 1187 keV and 1107 keV are clearly seen, while 80 keV below the energy threshold is not measured.

The observed number $N_{ij}(\theta_{12})$ of two γ -ray events with energies E_1 and E_2 detected in crystals i and j can be denoted as

$$N_{ij}(\theta_{12}) = N_0 r_{L,ij} \epsilon_i(E_1) \epsilon_j(E_2) W(\theta_{12}), \tag{1}$$

where N_0 is the number of two γ -ray events produced at the target, $r_{L,ij}$ is the dead time correction factor for the crystal pair (i, j) , which typically is on the order of 90%, $\epsilon_i(E_1)$ and $\epsilon_j(E_2)$ are the single photopeak efficiencies of the crystals i and j for γ -ray energies E_1 and E_2 , respectively, and $W(\theta_{12})$ is the angular correlation function between the two γ rays. If there is no angular correlation, then the angular correlation function is uniform, $W(\theta_{12}) = 1.0$, with respect to $\cos\theta_{12}$. The angular correlation function $W(\theta_{12})$ can be evaluated in an experiment using Eq. (1) as,

$$W(\theta_{12}) = C \sum_{i \neq j=0}^{14} \frac{N_{ij}(\theta_{12})}{\epsilon_i(E_1) \epsilon_j(E_2)}, \tag{2}$$

where C is a constant and the sum is taken over all possible combinations of (i, j) pairs having the angle θ_{12} . In the analysis, for every pair (i, j) of observed γ rays, we calculate $z = \cos\theta_{12}$ and fill the histogram at a position z with a weight $\frac{N_{ij}(\theta_{12})}{\epsilon_i(E_1) \epsilon_j(E_2)}$ given by the right-hand side of Eq. (2). An overall constant C in Eq. (2) is arbitrary in the present analysis, but if we evaluate the sum on the right-hand side of Eq. (2), it should be roughly equal to the number of two γ -ray events produced in the target. Any deviation from a uniform and constant distribution of $W(\theta_{12})$ with respect to $\cos\theta_{12}$ suggests the existence of an angular correlation between the two γ rays.

The calculation of the angular correlation function for the two γ rays from cascade transitions is based on the electromagnetic theory and quantum numbers conservation as given in Refs. [23–25]. The angular correlation function $W(\theta)$ is conveniently written in terms of Legendre polynomials as,

$$W(\theta) = \sum_{\ell=0}^{\ell_{\max}} A_{\ell} P_{\ell}(\cos\theta), \tag{3}$$

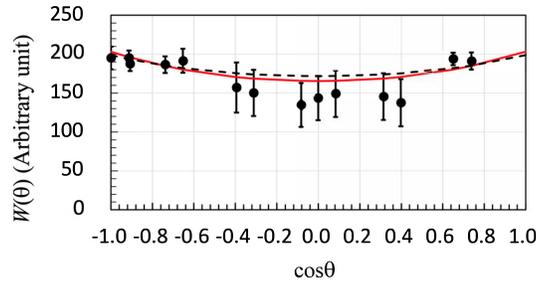


Fig. 5. Measurement of the angular correlation of the two γ rays of 1173 keV and 1332 keV from the cascade transition (2505 keV, $4^+ \rightarrow 1332$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{60}Ni in ^{60}Co β^- decay. The black dashed curve is calculated with theoretical values of $A'_2 = 0.102$ and $A'_4 = 0.0091$ in Eqs. (4) and (5). The red curve is the prediction with $A'_2 = 0.15$ and $A'_4 = 0.0091$. An overall normalization is arbitrary.

where $P_\ell(z)$ is a Legendre polynomial of a degree ℓ and A_ℓ is the coefficient. When the detectors for the two γ rays are placed (roughly) at cylindrically symmetrical positions from a given source point, this form is simplified to contain only leading order terms as $\ell = 0, 2$, and 4 , limiting transitions to dipole and quadrupole types, as

$$W(\theta) = C[1 + A_2 P_2(\cos\theta) + A_4 P_4(\cos\theta)], \quad (4)$$

where C is an overall constant. In any experiment, each γ -ray detector has a finite size and the angular correlation function is subject to correction for the finite size effect or the angular resolution effect [31,32]. If this effect is taken into account, the coefficients in Eq. (4) are written as,

$$A_2 = A'_2 Q_2 \quad \text{and} \quad A_4 = A'_4 Q_4, \quad (5)$$

where Q_2 and Q_4 are the correction factors, and A'_2 and A'_4 are the coefficients when each detector has a perfect angular resolution, namely $Q_2 = 1.0$ and $Q_4 = 1.0$. For the finite angular resolutions, Q_2 and Q_4 are less than 1.0 and the measured values for A_2 and A_4 become smaller than the theoretical values for A'_2 and A'_4 . The formulas and tabulated values for the coefficients, A'_2 and A'_4 , are given in Ref. [24]. The formulas for the correction factors Q_2 and Q_4 are also given in Refs. [31,32].

In our experiment, the angular correlation function $W(\theta)$ is analyzed using Eqs. (4) and (5) to determine the coefficients A'_2 and A'_4 . Then, the measured values, A'_2 and A'_4 , can be compared with the theoretical values, A'_2 and A'_4 [24]. In our ANNRI geometry, the correction factors are calculated to be $Q_2 = 0.93 \pm 0.01$ ($Q_2 = 0.94 \pm 0.01$) and $Q_4 = 0.77 \pm 0.01$ ($Q_4 = 0.80 \pm 0.01$) for $|\cos\theta| > 0.6$ ($|\cos\theta| < 0.4$), respectively. The uncertainty in the correction factors comes from the uncertainty in the dead layer thickness (1 mm) of the Ge crystal [33,34].

2.4. Angular correlation of the two γ rays from the cascade transition in ^{60}Co β^- decay

Figure 5 shows the angular correlation of the two γ rays of 1173 keV and 1332 keV from the cascade transition (2505 keV, $4^+ \rightarrow 1332$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{60}Ni from ^{60}Co β^- decay. We used only the data set of the M2H2 sample. In this analysis, the ^{60}Co source was set in the target position of the ANNRI detector. The predicted values for the coefficients are $A'_2 = 0.1020$ and $A'_4 = 0.0091$, respectively. The expected angular correlation is shown in the dashed black curve in Fig. 5 and it agrees well with the data, with $\chi^2/dof = 10.5/13$. If we fit the data using Eqs. (4) and (5) with A'_2 being a free parameter and with the fixed value of $A'_4 = 0.0091$, we obtain A'_2

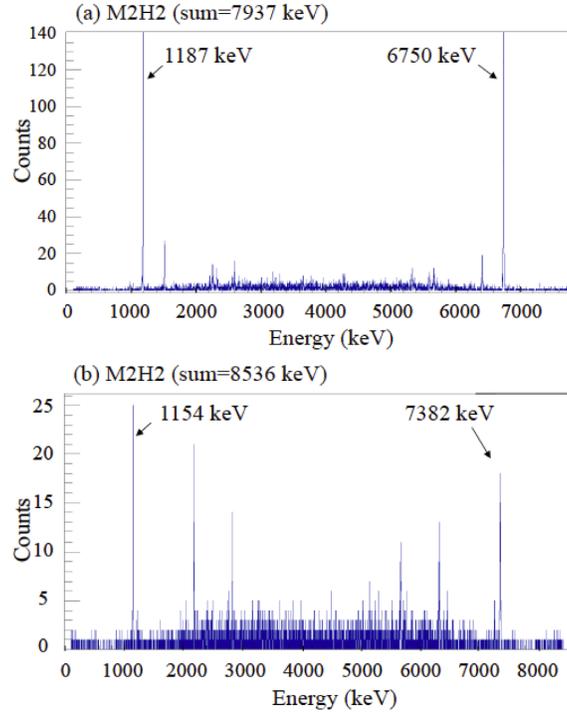


Fig. 6. (a) Selection of the two γ rays of 6750 keV and 1187 keV in the two-step cascade transition (7937 keV, $2^- \rightarrow 1187$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{158}Gd . (b) Selection of the two γ rays of 7382 keV and 1154 keV in the two-step cascade transition (8536 keV, $2^- \rightarrow 1154$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{156}Gd .

$= 0.15 \pm 0.06$ with $\chi^2/dof = 9.3/12$, which is consistent with the expected value 0.091 within the given uncertainty. The predicted curve is shown as a red solid curve in Fig. 5.

3. Analysis and result

3.1. Angular correlation of the two γ rays for prominent discrete cascade transitions

We now study the angular correlation of the two γ rays resulting from the prominent discrete cascade transitions of ^{158}Gd and ^{156}Gd nuclei.

The process of producing two γ rays of 6750 keV and 1187 keV, or 6750 keV and 1107 keV, in the cascade transition of ^{158}Gd was already shown in Fig. 4. Figures 6(a) and 6(b) exemplify the selection of the two γ rays in the M2H2 sample. We show in Fig. 6(a) the energy of the two γ rays (E_1 and E_2), in which the sum $E_1 + E_2$ is equal to 7937 keV within ± 25 keV in the M2H2 sample. We select the strongest two peaks at 6750 keV and 1187 keV where we observe almost no random background. The background rate estimation will be described later.

For the angular correlation function for the two γ rays of 6750 keV and 1187 keV in the two-step cascade transition (7937 keV, $2^- \rightarrow 1187$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{158}Gd , the expected coefficients are $A'_2 = 0.25$ and $A'_4 = 0$. In this cascade transition, the first transition is $E1$ and the second is $E2$. For the cascade transition including an $E1$ transition, A'_4 is expected to be 0.0 [24,25].

The angular correlation function measured for these two γ rays is shown in Fig. 7. We used two sets of events, namely the M2H2 sample (black closed circles) and the M2H3 sample (red closed squares). The data points have been corrected for efficiencies and acceptances according to Eq. (2). The error bars for all data points are calculated by adding the statistical and system-

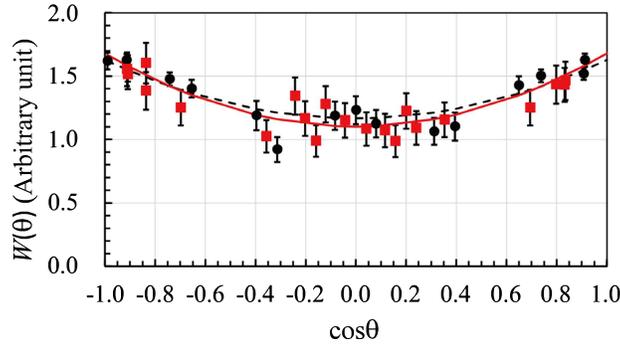


Fig. 7. Measurement of the angular correlation function for two γ rays of 6750 keV and 1187 keV in the two-step cascade transition ($7937 \text{ keV}, 2^- \rightarrow 1187 \text{ keV}, 2^+ \rightarrow 0 \text{ keV}, 0^+$) of ^{158}Gd . The data points of the M2H2 sample and the M2H3 sample are plotted in black closed circles and red closed squares, respectively. The prediction with $A'_2 = 0.31$ and that with the nominal value $A'_2 = 0.25$ are shown in the red solid curve and the black dashed curve, respectively. Both curves are consistent with the data.

atic uncertainties in quadrature. The data show a strong angular correlation between the two γ rays. If we fit the data using Eqs. (4) and (5) with A'_2 being a free parameter and a fixed value of $A'_4 = 0.0$, we obtain $A'_2 = 0.31 \pm 0.03$. The best fit result with $A'_2 = 0.31$ and $A'_4 = 0.0$ is shown in the red solid curve. The agreement between the fit and the data is good ($\chi^2/dof = 31/35$). The best fit values are consistent with the prediction of the expected value of 0.25 (shown in a black dashed curve) within about 2σ level.

At first glance, the energy distributions shown in Figs. 4 and 7(a) indicate that the background to this sample is negligible. However, we note that there is a chance that the cascade transition of 1107 keV and 80 keV can enter the same crystal, which results in a peak at 1187 keV. Its strength cannot be estimated by the extrapolation of the side-band background rates to the 1187-keV peak. In the following, we call this probability the coincidence summing probability. We estimated the coincidence summing probability to be about 5×10^{-3} by counting the number of events in the 7937-keV peak in ^{158}Gd data caused by the coincidence sum of the two γ rays of 6750 keV and 1187 keV ($7937 \text{ keV}, 2^- \rightarrow 1187 \text{ keV}, 2^+ \rightarrow 0 \text{ keV}, 0^+$). Similarly, the 8536-keV peak in ^{156}Gd data is caused by the coincidence sum of the two γ rays of 7382 keV and 1154 keV ($8536 \text{ keV}, 2^- \rightarrow 1154 \text{ keV}, 2^+ \rightarrow 0 \text{ keV}, 0^+$). The coincidence summing probability of the 8536-keV peak was found to agree with that of the 7937-keV peak in ^{158}Gd data within 20%. For both photopeaks, the direct $M2$ transition of the resonance state (2^-) to the ground state (0^+) is strongly suppressed, compared to the $E1$ transition from the resonance state (2^-) to the 1187-keV state (2^+ , ^{158}Gd) or to the 1154-keV state (2^+ , ^{156}Gd).¹ The coincidence summing probability of the 1187-keV peak is less than 1%. In addition, we checked all possible pairs of two γ rays in the M2H2 sample with a coincidence sum that aggregates to 6750 keV. Such pairs of the two γ rays include 5903 keV and 847 keV ($7937 \text{ keV}, 2^- \rightarrow 2034 \text{ keV}, 3^+ \rightarrow 1187 \text{ keV}, 2^+$) and 5784 keV and 966 keV ($7937 \text{ keV}, 2^- \rightarrow 2153 \text{ keV}, 2, 3^+ \rightarrow 1187 \text{ keV}, 2^+$). We estimated the coincidence summing probability to be about 1.5% of the total number of counts in the single photopeak of 6750 keV. The coincidence summing effect upon the angular correlation function is negligible.

¹We mistakenly listed the intensity of the 7937-keV peak as $0.55 \pm 0.03 (\times 10^{-2}\%)$ in Table 1 of our previous publication [21]. We used this intensity of the 7937-keV peak to estimate the coincidence summing probability in this paper.

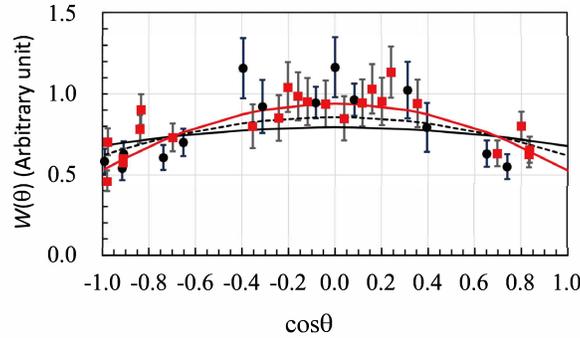


Fig. 8. Measurement of the angular correlation between two γ rays of 6750 keV and 1107 keV in the two-step cascade (7937 keV, $2^- \rightarrow 1187$ keV, $2^+ \rightarrow 80$ keV, 2^+) of ^{158}Gd . The data points of the M2H2 sample and the M2H3 sample are plotted in black closed circles and red closed squares, respectively. The predictions with $A'_2 = -0.11$ ($\delta = -9.0$), $A'_2 = -0.22$ ($\delta = -1.5$), and $A'_2 = -0.37$ are drawn in a black solid curve, black dashed curve, and red solid curve, respectively.

Next, the results for the angular correlation between the two γ rays of 6750 keV and 1107 keV in the cascade transition from ^{158}Gd (7937 keV, 2^-) are shown in Fig. 8. Note that the 80-keV γ ray in Fig. 4(right) cannot be detected by ANNRI since it is below our experimental threshold. The theoretical prediction for the angular correlation function is estimated for $E1-E2$ transition and for $E1-M1$ transition as,

$$A'_2 = -0.054, \quad A'_4 = 0 \text{ for a pure } E1 - E2 \text{ transition and,}$$

$$A'_2 = 0.175, \quad A'_4 = 0 \text{ for a pure } E1 - M1 \text{ transition.} \quad (6)$$

Figure 8 clearly shows a negative value for A'_2 . If we fit the data using Eqs. (4) and (5) with A'_2 being a free parameter and with a fixed value of $A_4 = 0.0$, we obtain $A'_2 = -0.37 \pm 0.04$. The agreement between the fit and the data is good with $\chi^2/dof = 38/35$. This fit value $A'_2 = -0.37 \pm 0.04$ is not consistent with the prediction of either a pure $E1-E2$ transition, or a pure $E1-M1$ transition. The best fit is shown as the red solid curve in Fig. 8. Previous measurement of the transition (1187 keV, $2^+ \rightarrow 80$ keV, 2^+) was performed in a Coulomb excitation experiment and it reported a mixture of $E2$ and $M1$ transitions with the mixture parameter $\delta = -9.0 \pm 1.5$ [35,36], where δ is defined as the ratio of $E2$ to $M1$ transition [23,24,37]. It is noted that the angular distribution is expected to show an interference effect caused by the mixture of two multipoles in a single transition. The coefficient A'_2 of the angular correlation function can be calculated [23,24,37] when the transition is mixed with a mixture parameter δ and it is given as

$$A'_2 = \frac{0.175 + 0.510\delta - 0.0536\delta^2}{1 + \delta^2}, \quad (7)$$

where $A'_4 = 0$, since the first transition is $E1$. The value of A'_2 is estimated by Eq. (7) to be -0.11 ± 0.01 for the previously reported value $\delta = -9.0 \pm 1.5$ and its prediction is drawn in the black solid curve in Fig. 8. Our data are inconsistent with this value.

If we fit the data with δ as a free parameter, we obtain $\delta = -1.5^{+1.5}_{-0.5}$, which gives $A'_2 = -0.22$ from Eq. (7). The prediction is barely consistent with the data. We note that the previous measurement of the transition was obtained by comparing the ratio of the 1107-keV rate at two different angles (0° and 90°) with respect to the beam [35]. The systematic effects in the previous experiment and in the present experiment which measured the angular correlation function at

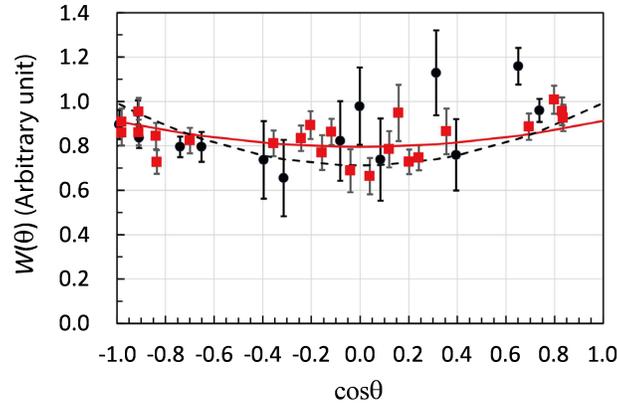


Fig. 9. Measurement of the angular correlation between two γ rays of 7382 keV and 1154 keV in the prominent two-step cascade transition (8536 keV, $2^- \rightarrow 1154$ keV, $2^+ \rightarrow 0$ keV, 0^+) for ^{156}Gd . The data points of the M2H2 sample and the M2H3 sample are plotted in black closed circles and red closed squares, respectively. The predictions with $A'_2 = 0.10$ (best fit, red solid curve) and that with the nominal value $A'_2 = 0.25$ (black dashed curve) are shown.

all angles are rather different. The background to our angular correlation analysis due to the coincidence summing effect is at the same level as that of Fig. 7 and is estimated to be negligible.

Figure 9 shows the angular correlation function for the prominent two γ rays of 7382 keV and 1154 keV in the two-step cascade transitions (8536 keV, $2^- \rightarrow 1154$ keV, $2^+ \rightarrow 0$ keV, 0^+) for ^{156}Gd . We show in Fig. 6(b) the energy of the two γ rays, in which the sum $E_1 + E_2$ is equal to 8536 keV within ± 25 keV in the M2H2 sample. We select the two peaks at 7382 keV and 1154 keV unambiguously. For this case, the theoretical prediction for the angular correlation function is the same as for the two-step cascade transition (7937 keV, $2^- \rightarrow 1187$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{158}Gd , but the result shown in Fig. 9 looks rather different from that of Fig. 7. If we fit the data using Eqs. (4) and (5) with A'_2 being a free parameter and with the fixed value of $A'_4 = 0.0$, we obtain $A'_2 = 0.10 \pm 0.04$ and the quality of the fit is relatively poor with $\chi^2/dof = 58/35$. The prediction with the theoretical value $A'_2 = 0.25$ is also shown as the black dashed curve.

We now consider the background levels to each peak of 1154 keV and 7382 keV. The background for the 1154-keV peak caused by the coincidence sum of 1075 keV and 79 keV is estimated to be 0.5%. We also checked all possible pairs of two γ rays in the M2H2 sample whose coincidence sum results in a peak at 7382 keV. We found that the number of pairs is more by about a factor of 5 than that for 6750 keV. The pairs of the two γ rays are 6345 keV and 1037 keV, which are produced in a cascade transition (8536 keV, $2^- \rightarrow 2191$ keV, $2^+ \rightarrow 1154$ keV, 2^+), 6745 keV and 637 keV, 6427 keV and 955 keV, 6381 keV and 901 keV, and 6319 keV and 1063 keV. We estimate the coincidence summing probability of all pairs to be about 7.7% of the total number of a single photopeak of 7382 keV. Thus, the background to the pairs of the two γ rays of 1154 keV and 7382 keV is estimated to be $8.2\% \pm 2.0\%$. Those backgrounds may have smeared the angular correlation function in addition to the poorer statistics of this sample than that of the ^{158}Gd data, as seen in Fig. 6.

3.2. Angular correlation of the two γ rays for the continuum

We also studied the angular correlation of the two γ rays emitted in the continuum transitions. In this analysis, we used only the two γ rays from the M2H2 sample for simplicity.

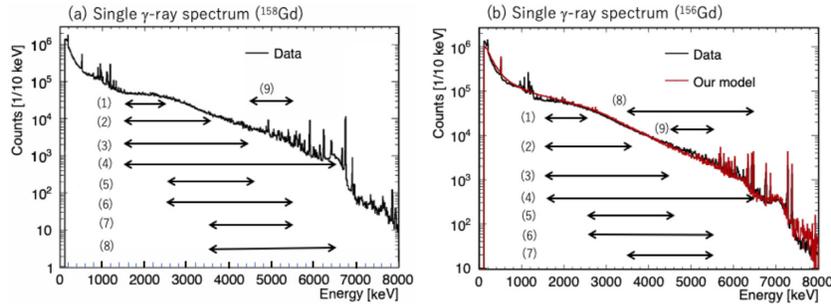


Fig. 10. Energy ranges (1)–(9) (E_1 – E_2) of the two γ rays are shown in arrows over the single energy spectrum of (a) ^{158}Gd and (b) ^{156}Gd . Figures 10(a) and 10(b) were taken from Fig. 4 ([21]) and Fig. 9(left) ([22]) of our previous publications, respectively.

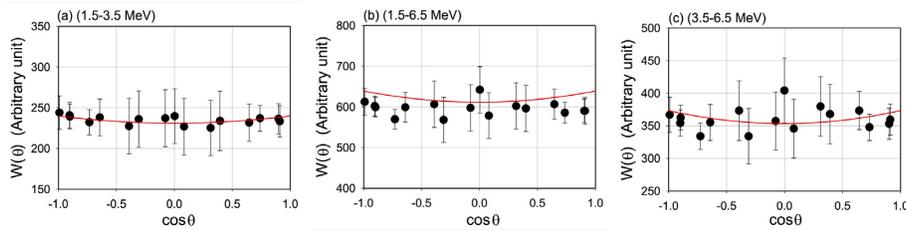


Fig. 11. Measurement of the angular correlation between two γ rays (E_1 and E_2) from the continuum for ^{158}Gd decays. The energy range for E_1 and E_2 is (a) 1.5–3.5 MeV, (b) 1.5–6.5 MeV, and (c) 3.5–6.5 MeV. The red lines show the best fit, which is consistent with a flat distribution.

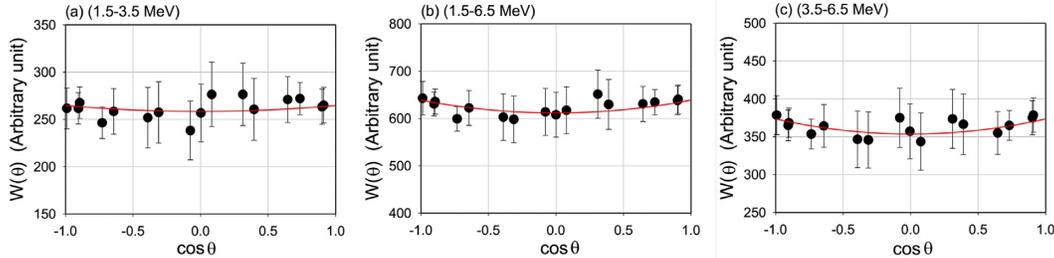


Fig. 12. Measurement of the angular correlation between two γ rays (E_1 and E_2) from the continuum for ^{156}Gd decays. The energy range for E_1 and E_2 is (a) 1.5–3.5 MeV, (b) 1.5–6.5 MeV, and (c) 3.5–6.5 MeV. The red lines show the best fit, which is consistent with a flat distribution.

In addition, we required that the energies of the two γ rays are within nine predefined energy ranges that avoid the energies of the strong discrete photopeaks that we have investigated above. The nine energy ranges ($a < E_1, E_2 < b$) are chosen as follows: a – b MeV = (1) 1.5–3.5 MeV, (2) 1.5–3.5 MeV, (3) 1.5–4.5 MeV, (4) 1.5–6.5 MeV, (5) 2.5–4.5 MeV, (6) 2.5–5.5 MeV, (7) 3.5–5.5 MeV, (8) 3.5–6.5 MeV, and (9) 4.5–5.5 MeV. They have been superimposed on the γ -ray spectra of $^{157}\text{Gd}(n, \gamma)$ and $^{155}\text{Gd}(n, \gamma)$ reactions in Fig. 10. Figures 10(a) and 10(b) were taken from Fig. 4 ([21]) and Fig. 9(left) ([22]) of our previous publications, respectively.

Figures 11 and 12 present exemplarily the results of angular correlation functions for the energy ranges (2), (4), and (7) for the ^{158}Gd and ^{156}Gd data. The error bars displayed in the figures include both statistical and systematic uncertainties. We analysed the angular correlation functions for all energy ranges, assuming a form $W(\theta) = C[1 + A_2P_2(\cos\theta)]$, where a constant C and the coefficient A_2 are the free parameters. The results for coefficient A_2 for all the en-

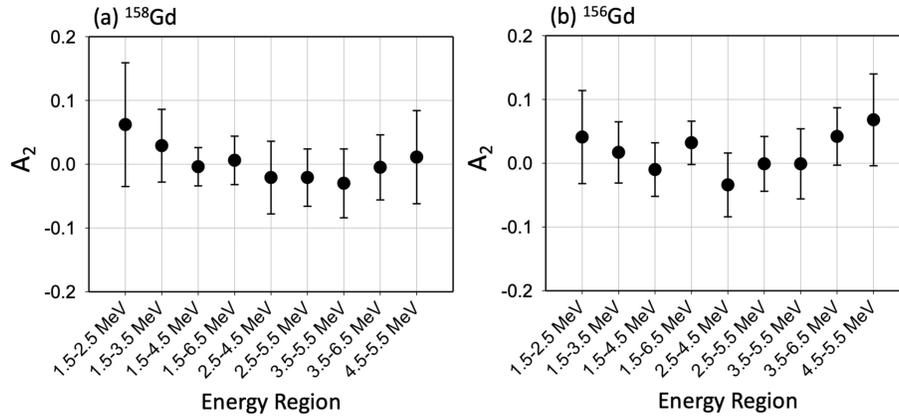


Fig. 13. Coefficient A_2 ((a) ^{158}Gd and (b) ^{156}Gd) of the angular correlation function plotted for various energy ranges (E_1-E_2) of the two γ rays in the continuum. The angular correlation function is assumed to be in the form of $W(\theta) = C[1 + A_2P_2(\cos\theta)]$. $A_2 = 0$ means no correlation.

ergy ranges are shown in Fig. 13, where the uncertainty of coefficient A_2 is determined by $\chi^2 = \chi_{\text{minimum}}^2 + 1.0$. The values of coefficient A_2 in any energy range are consistent with 0 within a few %. Hence, we observe no significant angular correlations for any combinations of two γ rays from the continuum.

4. Summary and discussion

Using the ANNRI Ge spectrometer setup at J-PARC, we have studied for the first time the angular correlations between the two γ rays emitted from ^{155}Gd and ^{157}Gd targets after capture of thermal neutrons.

We have shown that the angular correlation functions between the two prominent γ rays produced in the strong two-step cascade transitions from the resonance state can be described with the functional form of Eqs. (4) and (5) predicted by electromagnetic theory [23–25]. For the angular correlation function for the two γ rays of 6750 keV and 1187 keV in the two-step cascade transition (7937 keV, $2^- \rightarrow 1187$ keV, $2^+ \rightarrow 0$ keV, 0^+) of ^{158}Gd , our data shown in Fig. 7 are consistent with the prediction within 2σ level. The background to the angular correlation function is negligible.

Next, we showed in Fig. 8 the angular correlation function for the two γ rays of 6750 keV and 1107 keV in the cascade (7937 keV, $2^- \rightarrow 1187$ keV, $2^+ \rightarrow 80$ keV, 2^+) and compared it with the prediction of the electromagnetic theory. The best fit value to our data is not consistent with the prediction of either a pure $E1-E2$ transition, or a pure $E1-E1$ transition. The previous measurement of the transition (1187 keV, $2^+ \rightarrow 80$ keV, 2^+) reported a mixture of $E2$ and $M1$ transitions with a mixing parameter $\delta = -9.0 \pm 1.5$ [35]. Instead, our fit to the angular correlation function results $\delta = -1.5^{+1.5}_{-0.5}$, corresponding to $A_2 = -0.22$ from Eq. (7). Our result is not consistent with the previous measurement. We note that the previous measurement and the present experiment which measured the angular correlation function at all angles use different experimental methods. Further measurements will be necessary. The background to the angular correlation analysis in Fig. 8 due to a coincidence summing effect is again estimated to be negligible.

We also studied the angular correlation function for the two prominent γ rays of 7382 keV and 1154 keV in the two-step cascade transitions (8536 keV, $2^- \rightarrow 1154$ keV, $2^+ \rightarrow 0$ keV, 0^+) for

^{156}Gd in Fig. 9. For this case, the theoretical angular correlation function should be the same as the two-step cascade transition ($7937\text{ keV}, 2^- \rightarrow 1187\text{ keV}, 2^+ \rightarrow 0\text{ keV}, 0^+$) of ^{158}Gd , but the results shown in Fig. 9 are different from Fig. 7. We also checked all possible pairs of two γ rays in the M2H2 sample whose coincidence sum results in a peak at 7382 keV and found that the number of pairs is more by a factor of 5 than for 6750 keV . We estimated the coincidence summing probability of all pairs to be about 7.7% of the total number of a single photopeak of 7382 keV . Thus, the background to the pairs of the two γ rays of 1154 keV and 7382 keV is estimated to be $8.2\% \pm 2.0\%$. This background may have smeared the angular correlation function in addition to the poorer statistics of this sample than that of the ^{158}Gd data (Fig. 6).

Next, we have studied the angular correlations between two γ rays produced from the continuum transitions, assuming that the angular correlation can be written in a form $W(\theta) = C[1 + A_2P_2(\cos\theta)]$. We found that the value of the coefficient A_2 is consistent with 0 within uncertainties, typically 0.05 and less than 0.1, as shown in Fig. 13. Hence, we found no angular correlations for any two γ rays in the continuum for energies below 6.5 MeV .

This result agrees with our expectations since we picked random pairs of two γ rays in the cascade transition and excluded the prominent strong photopeaks from the pairs. The mean multiplicity of γ rays produced in the neutron capture reaction is about 5 for $E_\gamma > 0.2\text{ MeV}$. Since we pick a random pair of two γ rays in the continuum, the probability that the same pair is selected from the definite spin-parity states must be very small and, as a result, we expect that they show no angular correlations. We note that the γ rays from the continuum represent approximately 93% (97%) of the γ rays produced in the thermal neutron capture of the $^{157}\text{Gd}(n, \gamma)$ reaction ($^{155}\text{Gd}(n, \gamma)$ reaction) for $E_\gamma > 0.11\text{ MeV}$ [21,22].

In summary, our study of the angular correlation both for the two γ rays from the strong two-step cascade transition and for the randomly chosen two γ rays in the continuum is important information for the ongoing and future experiments using gadolinium for neutron tagging in a liquid-scintillator detector or in a water-Cherenkov detector.

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References

- [1] S. F. Mughabghab, Atlas of Neutron Resonances: Resonance Parameters and Thermal Cross Sections, $Z = 1-100$ (Elsevier, Amsterdam, 2006), 5th ed.
- [2] G. Leinweber, D. P. Barry, M. J. Trbovich, J. A. Burke, N. J. Drindak, H. D. Knox, R. V. Ballard, R. C. Block, Y. Danon, and L. I. Severnyak, Nucl. Sci. Eng. **154**, 261 (2006).
- [3] H. D. Choi et al. Nucl. Sci. Eng. **177**, 219 (2014).
- [4] M. Mastromarco et al., [n_TOF Collaboration], Eur. Phys. J. A **55**, 9 (2019).
- [5] Y. Abe et al., [Double Chooz Collaboration], Phys. Rev. Lett. **108**, 131801 (2012).
- [6] J. K. Ahn et al., [RENO Collaboration], Phys. Rev. Lett. **108**, 191802 (2012).
- [7] D. Adey et al. [Daya Bay Collaboration], Phys. Rev. Lett. **121**, 241805 (2018).
- [8] P. Adamson et al., [MINOS, MINOS+, Daya Bay Bugey-3], Phys. Rev. Lett. **125**, 071801 (2020).
- [9] Y. J. Ko et al., [NEOS Collaboration], Phys. Rev. Lett. **118**, 121802 (2017).
- [10] H. Almazán et al., [STEREO Collaboration], Phys. Rev. Lett. **121**, 161801 (2018);
- [11] H. Alekseev et al., [DANSS Collaboration], Phys. Lett. **B787**, 56 (2018).
- [12] A. P. Serebrov et al., [Neutrino-4 Collaboration], JETP Lett. **109**, 213 (2019).

- [13] S. Ajimura et al., [JSNS²-II Collaboration], (2020) [[arXiv:2012.10807](https://arxiv.org/abs/2012.10807)] [hep-ex] [[Search inSPIRE](#)].
- [14] S. Oguri, Y. Kuroda, Y. Kato, R. Nakata, Y. Inoue, C. Ito, and M. Minowa, Nucl. Instrum. Meth. A **757**, 33 (2014).
- [15] S. L. Ho, H. Yue, T. Tegafaw, M. Y. Ahmad, S. Liu, S.-W. Nam, Y. Chang, and G. H. Lee, ACS Omega **2022**, **7**, 2533.
- [16] K. Pushkin et al., [LZ Collaboration], Nucl. Instrum. Meth. A **936**, 162 (2019).
- [17] E. Aprile et al., (XENON Collaboration), JCAP **11**, 031 (2020).
- [18] J. F. Beacom and M. R. Vagins, Phys. Rev. Lett. **93**, 171101 (2004).
- [19] H. Sekiya (for Super-Kamiokande Collaboration), PoS **ICHEP2016**, 982 (2016).
- [20] L. Marti et al., [Super-Kamiokande Collaboration], Nucl. Instrum. Meth. A **959**, 163549 (2020).
- [21] K. Hagiwara et al., [ANNRI-Gd Collaboration], Prog. Theor. Exp. Phys. **2019**, 023D01 (2019).
- [22] T. Tanaka et al., [ANNRI-Gd Collaboration], Prog. Theor. Exp. Phys. **2020**, 043D02 (2020).
- [23] H. Frauenfelder, Annu. Rev. Nucl. Sci. **2**, 129 (1953).
- [24] I. C. Biedenharn and M. E. Rose, Rev. Mod. Phys. **25**, 729 (1953).
- [25] M. E. Rose, Elementary Theory of Angular Momentum (John Wiley & Sons, Inc., New York, 1957).
- [26] A. Chalil, T. Materna1, O. Litaize, A. Chebboubi, and F. Gunsing, Eur. Phys. J. A **58**, 30 (2022).
- [27] A. Kimura et al., J. Nucl. Sci. Technol. **49**, 708 (2012).
- [28] T. Kin et al., J. Korean Phys. Soc. **59**, 1769 (2011).
- [29] K. Kino et al., Nucl. Instrum. Meth. A **626**, 58 (2011).
- [30] K. Kino et al., Nucl. Instrum. Meth. A **736**, 66 (2014).
- [31] M. E. Rose, Phys. Rev. **91**, 610 (1953).
- [32] D. C. Camp and A. L. Van Lehn, Nucl. Instrum. Meth. **76**, 192 (1969).
- [33] H. Utsunomiya, H. Akimune, K. Osaka, T. Kaihori, K. Kurutaka, and H. Harada, Nucl. Instrum. Meth. A **548**, 455 (2005).
- [34] K. Terada et al., J. Nucl. Sci. Technol. **53**, 1881 (2005).
- [35] F. K. McGowan and W. T. Milner, Phys. Rev. C **23**, 1926 (1981).
- [36] N. Nica, Nucl. Data Sheets **141**, 326 (2017).
- [37] R. G. Arns and M. L. Wiedenbeck, Phys. Rev. **111**, 1631 (1958).