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Selection and application of factors for forecasting the epidemic time and severity of Japanese encephalitis prevalence

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Selection and application of factors for forecasting the epidemic time and severity of Japanese encephalitis prevalence*

Masana Ogata and Hirokazu Osaki

Abstract

For predicting median date or incidence rate in the prevalence of japanese encephalitis, the authors considered the 34 factors; namely, the climate, latitude, longitude, and date showing immunological positivity of hemagglutination inhibiting reaction on 50% the number of swine, etc. To make the mean square residual the smallest which yields, in the case of calculating with the multiple regression equation, the most important and meritorious factors were selected from the factors mentioned above by the voluntary selection rule devised by us. Multiple regression equations were formulated for them. To predict the median date in the prevalence of japanese encephalitis in whole japan, we found that the three factors, i. e. the amount of rainfall in April, the average temperature in March and HI positive rate of swine till the end of july, were essential. And for the foreseeing of incidence rate in Okayama Prefecture, factors concerning mosquitoes were added; this resulted in the useful two factors, namely, common logarithm of the total number of Culex tritaeniorhynchus till july 20th and the rainfall in June.

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Selection and Application of Factors for Forecasting the Epidemic Time and Severity of Japanese Encephalitis Prevalence

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Abstract: For predicting median date or incidence rate in the prevalence of Japanese encephalitis, the authors considered the 34 factors; namely, the climate, latitude, longitude, and date showing immunological positivity of hemagglutination inhibiting reaction on 50% the number of swine, etc. To make the mean square residual the smallest which yields, in the case of calculating with the multiple regression equation, the most important and meritorious factors were selected from the factors mentioned above by the voluntary selection rule devised by us. Multiple regression equations were formulated for them. To predict the median date in the prevalence of Japanese encephalitis in whole Japan, we found that the three factors, i.e. the amount of rainfall in April, the average temperature in March and HI positive rate of swine till the end of July, were essential. And for the foreseeing of incidence rate in Okayama Prefecture, factors concerning mosquitoes were added; this resulted in the useful two factors, namely, common logarithm of the total number of *Culex tritaeniorhynchus* till July 20th and the rainfall in June.

As to the route of the infection of Japanese encephalitis virus, it was thought that the virus propagates in swine (1) and herons (2). And mosquitoes bite swine and herons during viremia and change themselves to hazardous mosquitoes. In order to estimate the epidemic time curve of Japanese encephalitis patients, the onset time of hazardous mosquitoes is the most important.

And this onset time has a close correlation to the atmospheric temperature in summer; i.e. we call it "onset by high atmospheric temperature" (3–8). On the other hand, the time, when the immunological positivity of hemagglutination inhibiting reaction (HI reaction in short) of swine becomes positive to 50%, is also required for determining the onset of hazardous mosquitoes, as there is a close correlation between this time and the median date of epidemic time curve or the incidence rate (3–9).

In the present study we attempted to forecast the median date and the
incidence rate of Japanese encephalitis patients from average temperature every month, the duration of sunshine and the amount of rainfall as the climatic factors, latitude and longitude, date showing HI reaction on 50% of swine and HI positive rate on swine till the end of July. To make the mean square residual smallest, which yields, when calculated with the multiple regression equation, the most important and valuable factors from the various factors above mentioned (34 factors in all) by the voluntary selection rule devised by us. Multiple regression equations were formulated for them.

In addition, to examine the efficiency of the factor of the mosquitoes, we attempted to forecast the median date and the incidence rate in Okayama Prefecture based on the factors concerning the mosquitoes plus the factors above mentioned.

MATERIALS AND METHODS

I) Materials

In order to forecast the median date \( (Y_1) \) or the incidence rate \( (Y_2) \) in the prevalence of Japanese encephalitis, the authors considered the following factors in each prefecture from 1965 to 1970.

1) Climatic factors

<table>
<thead>
<tr>
<th>Month</th>
<th>average temperature ( (^\circ C/\text{day}) )</th>
<th>duration of sunshine ( (\text{hour}/\text{day}) )</th>
<th>amount of rainfall ( (\text{mmx}10^{-5}) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>January</td>
<td>( x_1 )</td>
<td>( x_{11} )</td>
<td>( x_{21} )</td>
</tr>
<tr>
<td>February</td>
<td>( x_2 )</td>
<td>( x_{12} )</td>
<td>( x_{22} )</td>
</tr>
<tr>
<td>March</td>
<td>( x_3 )</td>
<td>( x_{13} )</td>
<td>( x_{23} )</td>
</tr>
<tr>
<td>April</td>
<td>( x_4 )</td>
<td>( x_{14} )</td>
<td>( x_{24} ) (this)</td>
</tr>
<tr>
<td>May</td>
<td>( x_5 )</td>
<td>( x_{15} )</td>
<td>( x_{25} ) (year)</td>
</tr>
<tr>
<td>June</td>
<td>( x_6 )</td>
<td>( x_{16} )</td>
<td>( x_{26} )</td>
</tr>
<tr>
<td>July</td>
<td>( x_7 )</td>
<td>( x_{17} )</td>
<td>( x_{27} )</td>
</tr>
<tr>
<td>October</td>
<td>( x_8 )</td>
<td>( x_{18} )</td>
<td>( x_{28} )</td>
</tr>
<tr>
<td>November</td>
<td>( x_9 )</td>
<td>( x_{19} )</td>
<td>( x_{29} ) (previous)</td>
</tr>
<tr>
<td>December</td>
<td>( x_{10} )</td>
<td>( x_{20} )</td>
<td>( x_{30} ) (year)</td>
</tr>
</tbody>
</table>

2) latitude : \( x_{31} \)
3) longitude : \( x_{32} \)
4) date showing HI reaction on 50% number of swine : \( x_{33} \)
5) positive rate on swine till the end of July : \( x_{34} \)

Median date and date showing HI reaction on 50% of swine were
Factors for Predicting J. E. Prevalence

expressed as days counted from June 20th.

The following factors were used to forecast the median date or the incidence rate on Okayama Prefecture in order to examine the efficiency of the factor of mosquitoes.

6) The number of Culex tritaeniorhynchus (C. t. in short)

- common logarithm of $\frac{3}{5} \text{ C. t. till July 10th} : x_{35}$
- common logarithm of $\frac{3}{5} \text{ C. t. till July 10th} : x_{36}$
- common logarithm of $\frac{3}{5} \text{ C. t. till the end of July} : x_{37}$
- common logarithm of $\frac{3}{5} \text{ C. t. till the end of July} : x_{38}$
- common logarithm of $\frac{3}{5} \text{ C. t. till August 10th} : x_{39}$
- common logarithm of $\frac{3}{5} \text{ C. t. till August 10th} : x_{40}$

II) Methods

The multiple regression equation was calculated as follows.

$$y: \text{the dependent variable}$$

$$x=(x_1, x_2, \ldots, x_k): \text{the independent variable}$$

$$(y_i, x_i), x_i=(x_{i1}, x_{i2}, \ldots, x_{ik}) : \text{the observation}$$

$$i=1, 2, \ldots, N \text{ of } (y, x)$$

Then the multiple regression equation became as follows.

$$\hat{y}=\bar{y} + \sum_{i=1}^k \beta_i(x_i - \bar{x_i})$$

Where

$$\hat{d}=(d_1, d_2, \ldots, d_k)' , \quad S=(s_{ij})$$

$$d_j=\sum_{i=1}^N (y_i-\bar{y})(x_{ji}-\bar{x_j}), \quad j=1, 2, \ldots, k$$

$$s_{ij}=\sum_{i=1}^N (x_{ii}-\bar{x_i})(x_{jj}-\bar{x_j}), \quad i, j=1, 2, \ldots, k$$

then $(\beta_1, \beta_2, \ldots, \beta_k)=\hat{d}'S^{-1}$.

The mean square residual from the multiple regression was as follows.

$$\hat{\sigma}^2=\frac{\sum_{i=1}^N (y_i-\hat{y})^2 - \hat{d}'S^{-1}\hat{d}}{(N-k-1)} \ldots \ldots (1)$$

If it would be possible to select the important and meritorious factors from many various factors used in the multiple regression, then we can explain clearly the tendency of the dependent variable with those selected factors alone.

In equation (1), the smaller the mean square residual became, the better the efficiency of the multiple regression equation was. $\sum_{i=1}^N (y_i-\bar{y})^2$ in (1) was not connected with independent variables. Then the relation between $\hat{d}'S^{-1}\hat{d}$ and the individual independent variable was examined.
\[ U = (r_{ij}) \]
\[ \tilde{\delta} = (\delta_1, \delta_2, \ldots, \delta_k)' \]

\[ \tilde{\delta} = (\delta_1, \delta_2, \ldots, \delta_k)' \]
\[ \tilde{\delta} \]
\[ \tilde{\delta} = (\delta_1, \delta_2, \ldots, \delta_k)' \]

\[ \tilde{U}^{-1}\tilde{\delta} = \tilde{\delta}U^{-1}\theta \quad \ldots \quad (2) \]

Further

\[ \tilde{U}^{-1}\tilde{\delta} = \delta_i + (\delta_2 - \gamma_{ij}\delta_i)/(1 - \gamma_{ij}) + \ldots \]
\[ + \alpha_j\delta_i + \ldots + \ldots \]

where \[ \alpha_j > 0 \quad j = 1, 2, \ldots, k \]

\[ \alpha_j \quad j = 1, 2, \ldots, k \]

Therefore, the value of \[ \tilde{d}'S^{-1}\tilde{d} \]

increased with the increase of the number of independent variables. Thus we considered the selection method of independent variables by which the value of \[ \tilde{d}'S^{-1}\tilde{d} \]

attained maximum in some sense.

II 2.1) Forward selection method (F. S. M.)

II 2.1.1) \( j = 1 \) (only one independent variable)

Only one independent variable was selected from \( k \) independent variables.

From equations (2) and (3),

\[ \tilde{d}'S^{-1}\tilde{d} = \delta_i^2 \]

The criterion of selection was determined as follows.

\[ \max_{\delta_i} \tilde{d}'S^{-1}\tilde{d} = \max_{\delta_i} \delta_i^2, \quad i \in \{1, 2, \ldots, k\} \]
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$I_1$ was taken as the independent variable number which satisfied the above equation. The regression equation calculated from $I_1$ variable was most efficient.

2.1.2) $j = 2$ (two independent variable)

Two independent variables were selected from $k$ independent variables. In this case, one independent variable was fixed on $I_1$. Then equation (2) and (3) became as follows.

$$\tilde{d}' S^{-1} \tilde{d} = \tilde{d}_1^2 + \left( \tilde{d}_2 - \gamma_{11} \tilde{d}_1 \right)^2 / \left( 1 - \gamma_{22} \right)$$

The criterion was as follows.

$$\max_{i_2} \tilde{d}' S^{-1} \tilde{d} = \max \left\{ \tilde{d}_1^2 + \left( \tilde{d}_2 - \gamma_{11} \tilde{d}_1 \right)^2 / \left( 1 - \gamma_{22} \right) \right\}$$

$$i_2 \in \{ 1, 2, \ldots, k \} - \{ I_2 \}.$$  

$I_2$ was put as the selected independent variable number. Thus the regression equation using $I_1$ and $I_2$ variables was more efficient than any other ones doing other two variables.

2.1.3) $j = m$ (in general case)

$d'_S S^{-1} \tilde{d} (i_1, i_2, \ldots, i_m)$ was put as the value of $d'_S S^{-1} \tilde{d}$ calculated from independent variables $i_1, i_2, \ldots, i_m$.

Independent variables $I_1, I_2, \ldots, I_{m-1}$ were already selected before this step. Then $I_m$ satisfied the following equation.

$$\max_{i_m} d'_S S^{-1} \tilde{d} (I_1, I_2, \ldots, I_{m-1}, i_m)$$

$$i_m \in \{ 1, 2, \ldots, k \} - \{ I_1, I_2, \ldots, I_{m-1} \}$$

Then the regression equation was made using $I_1, I_2, \ldots, I_m$ variables. The order of the independent variable by forward selection method was $I_1, I_2, \ldots, I_j, \ldots, I_k$.

And the efficiency of individual variable decreased with the increase of $j$.

2.2) Backward selection method (B.S.M.)

$D_{j}(m)$ was taken as the value of $d'_S S^{-1} \tilde{d}$ calculated from independent variables which consisted of independent variables $(i_1, i_2, \ldots, i_m)$ minus variable $i_j$.

In this selection method, the variable of which efficiency was the lowest was selected one by one.

2.2.1) $m = k$

In this step, the unnecessary independent variable was selected from $k$ independent variables by the following criterion.
max \( D_j(k), j \in \{1, 2, \ldots, k\} \).

\( I'_k \) was taken as the selected independent variable number. \( I'_k \) had a lower efficiency for the multiple regression equation than any other variables.

2, 2, 2) \( m=1 \)

\( I'_{k-1}, I'_{k-2}, \ldots, I'_{k-1} \) were already selected before this step. Then \( I_1 \) was taken as the independent variable number selected by the following criterion.

\[
\max d_j(1), j \in \{1, 2, \ldots, k\} - \{I_{k+1}, I_{k+2}, \ldots, I_k\}.
\]

In step \( m \), the regression equation was made using \( \{I, 2, \ldots, k\} - I_{m+1}, I_{m+2}, \ldots, I'_k \).

This process continued until \( m=1 \). The efficiency of individual variable increased with the decrease of \( m \).

2, 3) All possible selection method (A.P. S. M.)

In this method, the combination of variables of which efficiency was the highest among many variables was selected.

\( I'_1, I'_2, \ldots, I'_m \) were taken as the combination of variables selected by the following criterion.

\[
\max \tilde{d}^{-1} \tilde{d}(i_1, i_2, \ldots, i_m), (i_1, i_2, \ldots, i_m) \in \{1, 2, \ldots, k\}.
\]

\( (i_1, i_2, \ldots, i_m) \)

In each step, the regression equation was made using \( I'_1, I'_2, \ldots, I'_m \).

In the case of \( m=1 \), \( I'_1=I'_1 \).

In the case of \( m=k-1 \), \( I'_1^{-1}, I'_2^{-1}, \ldots, I'_{k-1}^{-1} = \{I'_1, I'_2, \ldots, I'_{k-1}\} \)

All possible selection methods had logically higher efficiency than other two selection methods. But this method required the longest computation time.

RESULTS AND DISCUSSION

1) Estimation of median dates of epidemic time curve of patients in Japan

1, 1) Estimation from the average atmospheric temperature

The correlation matrix, mean value and unbiased variance are shown in Table 1.

The correlation coefficient between median date and average atmospheric temperature in May (x_5) was -0.830. The absolute value was greater than any other coefficients. Then x_5 became the most important factor to estimate the median date. The results of forward (F.S.M.), backward (B.S.M.) and all possible selection methods (A.P.S.M.) are shown in Table 2. In the case of one factor, the average atmospheric temperature in May (x_5) was most useful among 10 factors from the results of three selection methods. And the regression equation becomes as follows.

\[
y_1 = -101.006x_5 + 289.120,
\]

\( \hat{\sigma} = 11.99 \).................(1)
Factors for Predicting J.E. Prevalence

Table 1: Correlation coefficients between mean values and unbiased variances

<table>
<thead>
<tr>
<th></th>
<th>Y1</th>
<th>X1</th>
<th>X2</th>
<th>X3</th>
<th>X4</th>
<th>X5</th>
<th>X6</th>
<th>X7</th>
<th>X8</th>
<th>X9</th>
<th>X10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y1</td>
<td>1.000</td>
<td>-0.123</td>
<td>0.134</td>
<td>0.759</td>
<td>-0.251</td>
<td>-0.830</td>
<td>0.747</td>
<td>-0.742</td>
<td>0.749</td>
<td>0.771</td>
<td></td>
</tr>
<tr>
<td>X1</td>
<td>1.000</td>
<td>0.535</td>
<td>-0.020</td>
<td>0.671</td>
<td>0.377</td>
<td>-0.076</td>
<td>0.350</td>
<td>0.015</td>
<td>0.087</td>
<td>0.182</td>
<td></td>
</tr>
<tr>
<td>X2</td>
<td>1.000</td>
<td>0.365</td>
<td>0.381</td>
<td>-0.066</td>
<td>0.283</td>
<td>0.195</td>
<td>0.314</td>
<td>0.403</td>
<td>0.480</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X3</td>
<td>1.000</td>
<td>0.109</td>
<td>-0.718</td>
<td>0.989</td>
<td>-0.484</td>
<td>0.989</td>
<td>0.989</td>
<td>0.938</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X4</td>
<td>1.000</td>
<td>0.512</td>
<td>0.078</td>
<td>0.539</td>
<td>0.128</td>
<td>0.151</td>
<td>0.128</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X5</td>
<td>1.000</td>
<td>-0.697</td>
<td>0.833</td>
<td>-0.675</td>
<td>-0.702</td>
<td>-0.650</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X6</td>
<td>1.000</td>
<td>-0.471</td>
<td>0.991</td>
<td>0.970</td>
<td>0.932</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X7</td>
<td>1.000</td>
<td>-0.466</td>
<td>-0.489</td>
<td>-0.462</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X8</td>
<td>1.000</td>
<td>0.981</td>
<td>0.943</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X9</td>
<td>1.000</td>
<td>0.957</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X10</td>
<td>1.000</td>
<td>1.000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>


Unbiased variance: 455.914 | 2.160 | 3.808 | 100.487 | 1.353 | 3.079 | 71.381 | 0.934 | 40.725 | 30.667 | 35.542 |

N=72

Table 2: Results of forward, backward and all possible selection methods from the data of Table 1.

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
</table>

This equation (1) was more efficient than any other ones calculated from average atmospheric temperature in other months to forecast the median date. In the case of two factors, the average atmospheric temperature in May ($x_5$) and December in previous year ($x_{10}$) were most useful among 10 factors. And the multiple regression equation became as follows.
In the case of three factors, the result of F. S. M. coincided with that of A. P. S. M. Generally the results of all possible selection methods were logically more useful than those of other two methods. Then two factors mentioned above, besides the average atmospheric temperature in July, were most useful.

\[ Y_1 = -6.931x_5 + 1.435x_{10} - 206.101 \]
\[ \hat{\sigma} = 10.12 \]  \hspace{1cm} (2)

In the case of four factors, average atmospheric temperature in February, May, June and previous year's December were selected from B. S. M. and A. P. S. M.

\[ Y_1 = -3.828x_5 - 6.118x_7 + 1.571x_{10} + 234.441 \]
\[ \hat{\sigma} = 9.65 \]  \hspace{1cm} (3)

The root of the mean square residual decreased gradually with the increase of the number of factors up to 7 factors, and after that it increased with the increase in the number of factors in B. S. M. and A. P. S. M. methods. From these results, obviously the average atmospheric temperature in January, February, March, May, June, and previous year's December was most efficient to estimate the median date in the prevalence of Japanese encephalitis in whole Japan. And the most useful regression equation became as follows,

\[ Y_1 = -2.478x_2 - 6.602x_5 - 1.108x_6 + 3.351x_{10} + 243.441 \]
\[ \hat{\sigma} = 9.48 \]  \hspace{1cm} (4)

1, 2) Estimation from 34 factors

The results of A. P. S. M. are shown in Table 3. Time to calculate

<table>
<thead>
<tr>
<th>number of variable</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>R</th>
<th>( \hat{\sigma} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>X_5</td>
<td>-10.101</td>
<td>244.874</td>
<td>11.99</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X_3</td>
<td>1.724</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>X_4</td>
<td>-113.514</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X_2</td>
<td>-84.254</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X_1</td>
<td>-0.129</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X_0</td>
<td>52.510</td>
<td>52.510</td>
<td>8.65</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X_5</td>
<td>2.304</td>
<td></td>
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</tr>
<tr>
<td>X_4</td>
<td>-53.868</td>
<td></td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>X_3</td>
<td>-0.121</td>
<td></td>
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<td>X_2</td>
<td>124.503</td>
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<td></td>
</tr>
<tr>
<td>X_1</td>
<td>8.25</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>incidence rate</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>R</th>
<th>( \hat{\sigma} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>X_5</td>
<td>0.716</td>
<td></td>
<td></td>
<td></td>
<td>-4.159</td>
<td>2.353</td>
</tr>
<tr>
<td>X_5</td>
<td>0.729</td>
<td>-1.022</td>
<td></td>
<td></td>
<td>11.560</td>
<td>2.045</td>
</tr>
<tr>
<td>X_4</td>
<td>-1.041</td>
<td></td>
<td></td>
<td></td>
<td>11.760</td>
<td>1.904</td>
</tr>
<tr>
<td>X_4</td>
<td>-0.544</td>
<td></td>
<td></td>
<td></td>
<td>27.091</td>
<td>1.838</td>
</tr>
</tbody>
</table>

Table 3 Selected factors by all possible selection methods and regression coefficients.
Factors for Predicting J.E. Prevalence

A. P. S. M. took too long in more than 5 factors that the calculation was stopped up to 4 factors. The results of F. S. M. and B. S. M. were used to examine the degree of the efficiency of the multiple regression equation in more than May ($x_5$) was selected. This factor was the most useful among 34 factors chosen. Then the regression equation was equal to the equation (1). In case of two factors, the average atmospheric temperature in March ($x_3$) and rainfall amount in April ($x_{24}$) were selected. And the regression equation became as follows.

$$\hat{y}_1 = 1.724x_3 - 113.61x_{24} + 50 + 50.355 \quad \hat{\sigma} = 9.59$$ \hspace{1cm} (6)

The efficiency of this equation was about equal to that of equation (3). The mean square residual decreased with the increase of the number of factors up to 4 factors. Then the multiple regression equation was calculated using four factors, that is, the rainfall in April ($x_{24}$), the average atmospheric temperature in May ($x_5$) and in previous year's November ($x_9$), and positive rate on swine till the end of July ($x_{34}$) were useful to estimate the median date.

$$\hat{y}_1 = -3.095x_5 + 2.303x_9 - 53.868x_{24} - 0.121x_{34} + 124.503 \quad \hat{\sigma} = 8.25$$ \hspace{1cm} (7)

This (equation 7) was more efficient than any other equations above mentioned. Then it became clear that the climatic factors and the factors of HI reaction of swine were useful and beneficial to estimate the median date.

The root of mean square residual calculated by 12 factors ($x_2, x_5, x_6, x_{10}, x_{11}, x_{14}, x_{15}, x_{19}, x_{24}, x_{25}, x_{28}, x_{31}, x_{34}$) from the backward selection method was 7.75, which was the smallest.

$$\hat{y} = -4.532x_2 + 5.201x_3 - 4.159, a = 2.35 \hspace{1cm} \hat{\sigma} = 7.75$$ \hspace{1cm} (8)

The difference between $\sigma$ of (equations 7 and 8) was 0.5. Then if we wanted to estimate the median date roughly, the equation (7) was the most useful.

2) Estimation of incidence rate of Japanese encephalitis from 34 factors.

The results of A. P. S. M. were shown in Table 3. The factor of the average atmospheric temperature also played an important roll for the estimation of the incidence rate.

In case of one factor, the average atmospheric temperature in March ($x_3$) was selected. And the regression equation became as follows.

$$\hat{y} = 0.716x_3 - 4.159 \quad \hat{\sigma} = 2.35$$ \hspace{1cm} (9)

The average atmospheric temperature was the most useful to estimate the median date or the incidence rate in the case of only one factor.

The efficiency of the multiple regression of the incidence rate increased with increase in the number of factors up to 4 factors.
M. Ogata and H. Osaki

TABLE 4 FACTORS USED FOR ESTIMATION OF MEDIAN DATE AND MORBIDITY RATE

<table>
<thead>
<tr>
<th>x35</th>
<th>x36</th>
<th>x37</th>
<th>x38</th>
<th>x39</th>
<th>x40</th>
<th>x33</th>
<th>x34</th>
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<td>2.02</td>
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<td>3.07</td>
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<td>3.18</td>
<td>2.88</td>
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<tr>
<td>42</td>
<td>1.80</td>
<td>1.75</td>
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<td>3.69</td>
<td>3.85</td>
<td>3.75</td>
<td>36</td>
</tr>
<tr>
<td>43</td>
<td>2.04</td>
<td>2.00</td>
<td>3.60</td>
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<td>63</td>
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<td>44</td>
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<td>2.55</td>
<td>48</td>
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<tr>
<td>45</td>
<td>1.08</td>
<td>0.48</td>
<td>1.97</td>
<td>1.11</td>
<td>2.20</td>
<td>1.41</td>
<td>65</td>
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<td>1.11</td>
<td>2.50</td>
<td>1.89</td>
<td>2.54</td>
<td>1.27</td>
<td>58</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>x35</th>
<th>x36</th>
<th>x37</th>
<th>x38</th>
<th>x39</th>
<th>x40</th>
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</thead>
<tbody>
<tr>
<td>41</td>
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</tr>
<tr>
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<td>2.71</td>
<td>2.98</td>
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<td>2.73</td>
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<tr>
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<td>2.30</td>
<td>1.82</td>
<td>2.20</td>
<td>1.83</td>
<td>64</td>
</tr>
</tbody>
</table>

Then the useful regression equation was that of four factors.
\[ \hat{y}_2 = 0.362x_2 + 0.721x_3 - 1.522x_4 - 0.269x_{32} + 27.091 \]
\[ \hat{\sigma} = 1.84 \]

And the useful factors were the average atmospheric temperature in February (x2), in March (x3) and in April (x4), and the longitude (x32).

Further from the result of backward selection method, the following regression equation of incidence rate attained the lowest value of the mean square residual.
\[ \hat{y} = -1.297x_1 + 1.562x_2 + 0.551x_3 - 1.718x_4 + 1.259x_9 - 0.836x_{10} \]
\[-0.865x_{15} + 0.893x_{16} - 0.828x_{18} - 0.453x_{20} + 11.859x_{21} + 3.284x_{26} \]
\[-19.831x_{29} - 0.265x_{32} + 0.026x_{33} + 27.590 \]
\[ \hat{\sigma} = 1.65 \]

Therefore, the multiple regressions (equations 10 and 11) were the most useful to estimate the incidence rate of Japanese encephalitis.

3) Estimation from climatic factors added with factors concerning mosquitoes in Okayama Prefecture.

As to the route of the infection of Japanese encephalitis virus, it was thought that the mosquitoes played an important role in the virus propagation. Then it was necessary to take into consideration the factor of mosquitoes to forecast the median date or incidence rate of the encephalitis. But there was such a great difference among the data, i.e. common logarithms of the numbers, of mosquitoes (\textit{Culex tritaeniorhynchus}, C. t, in short) in each prefectures that the efficiency of the factor of C. t. was examined only in Okayama Prefecture. Table 4 shows the factors used and the data. Fourteen variables used are x6, x7, x16, x17, x26, x27, x33 and x34 and variables from x35 to
Factors for Predicting J.E. Prevalence

**PREVALENCE OF JAPANESE ENCEPHALITIS IN OKAYAMA PREFECTURE (1966~1971)**

<table>
<thead>
<tr>
<th>x_6</th>
<th>x_7</th>
<th>x_10</th>
<th>x_17</th>
<th>x_26</th>
<th>x_27</th>
<th>Median incidence</th>
<th>Incidence rate</th>
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<td>224.5</td>
<td>140.0</td>
<td>168.5</td>
<td>198.0</td>
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<td>26.2</td>
<td>274.9</td>
<td>226.5</td>
<td>191.5</td>
<td>53</td>
<td>1.0</td>
<td></td>
</tr>
<tr>
<td>21.7</td>
<td>25.1</td>
<td>102.0</td>
<td>250.5</td>
<td>185.3</td>
<td>152.3</td>
<td>69</td>
<td>1.0</td>
</tr>
<tr>
<td>20.5</td>
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<td>291.5</td>
<td>267.0</td>
<td>201.9</td>
<td>183.6</td>
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<tr>
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<td>329.0</td>
<td>137.0</td>
<td>96.5</td>
<td>190.6</td>
<td>-</td>
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</tr>
<tr>
<td>22.1</td>
<td>26.5</td>
<td>168.0</td>
<td>272.5</td>
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<tr>
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<tr>
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<td>168.1</td>
<td>67</td>
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<tr>
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<tr>
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<td>404.5</td>
<td>140.0</td>
<td>157.2</td>
<td>-</td>
<td>0</td>
</tr>
</tbody>
</table>

Clearly there is a difference between the data of C. t. in southern part and those of northern part in Okayama Prefecture. Then the data from 1966 to 1971 in southern and northern parts of Okayama Prefecture were used for calculation.

3.1) Median date

In this calculation, the number of data was 8 and that of independent variables was 14. The number of independent variables was more than that of data. Then the mean square residual of regression equation decreased with the increase in the number of independent variables. But the accuracy of estimating data in the other years became poorer with the increase of factors. Therefore, the results up to four factors were mainly explained. In the case of one factor, the duration of sunshine in July (x_17) was the most important factor. The factor of mosquitoes played an important role in case of more than two factors (Table 5).

In the case of two factors, the duration of sunshine in July (x_17) and number of C. t. (♀ + ♂) till July 10th (x_26) were selected. In the case of three or four factors, the number of C. t. (♀) till July 10th (x_26) and the climatic factors were selected from 14 factors.

From these results, it is clear that the factors of mosquitoes and of the climate are necessary to estimate the median date of epidemic time curve.

3.2) Incidence rate

In the case of one factor, the number of C. t. (♀ + ♂) till July 10th (x_26) was most important to estimate the incidence rate. In two factors, the number of C. t. (♀ + ♂) till July 10th and the rainfall in June (x_28) were most important. In three factors, only the climatic factors were important.
for estimating the incidence rate. Therefore, when the number of C. t. could not be measured, the multiple regression equation calculated by these three factors was most efficient to estimate the incidence rate. In four factors, only those factors concerned with the number of C. t. were selected. Thus, when the number of C. t. only is measured, the multiple regression equation calculated by these four factors can be used to estimate the incidence rate in Okayama Prefecture. From these results, it is evident that the factor of mosquitoes plays an important role in estimating the median date and the incidence rate in Okayama Prefecture. Therefore, when it is possible to gather the data regarding the factor of mosquitoes in all Japan prefectures, the estimation of median date and incidence rate of Japanese encephalitis will become more accurate. Precise comparison of values of median date or incidence rate estimated by this method with their actual values will be reported in the near future.

REFERENCES


Factors for Predicting J.E. Prevalence

614-619, 1959


